



# Electron spin resonance spectroscopy of molecules in large precessional motion: A case of $\text{H}_6^+$ and $\text{H}_4\text{D}_2^+$ in solid parahydrogen

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## ABSTRACT

We have measured electron spin resonance (ESR) spectra of  $\text{H}_6^+$  and  $\text{H}_4\text{D}_2^+$  ions produced in  $\gamma$ -ray irradiated solid parahydrogen. Anisotropic hyperfine-coupling constants for  $\text{H}_6^+$  and  $\text{H}_4\text{D}_2^+$  determined by the analysis of ESR lines at 4.2 K were  $-0.06$  and  $-0.12$  mT, respectively, which were opposite in sign to and much smaller than theoretical results of 1.17–1.25 mT. Although no change was observed in  $\text{H}_6^+$ , the constant for  $\text{H}_4\text{D}_2^+$  increased to be 1.17 mT at 1.7 K, which is very close to the theoretical value. We concluded that  $\text{H}_6^+$  both at 4.2 and 1.7 K and  $\text{H}_4\text{D}_2^+$  at 4.2 K should be in a large precessional motion with the angle of  $57$ – $59^\circ$ , but the precession of  $\text{H}_4\text{D}_2^+$  is stopped at 1.7 K.

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## 1. Introduction

Study of rotational and librational motions of molecules trapped in cryocrystals has a long history [1–14]. The study was mainly carried out using infrared absorption spectroscopy (IR); however, electron spin resonance (ESR) spectroscopy is also useful [9–13]. Advantage of ESR over IR is that ESR measures pure rotational and librational motions, whereas IR induces ro-vibrational transitions.

When rotation of radicals in cryocrystals is hindered or stopped, ESR lines are broadened via anisotropic  $g$ -values and hyperfine interactions. On the contrary, when radicals rotate freely, such a broadening disappears due to motional narrowing [11,12]. Kumada [13] found by analysis of ESR lines of  $\text{O}_2$  in isotopic solid hydrogens that the librational amplitude does not decrease but increases with an increase in pressure. This result indicates that cage distortion rather than size of cage is important factor which determines the librational motion [14].

In order to study the rotational and librational motions, highly resolved ESR lines are essential. Solid para- $\text{H}_2$  ( $p\text{-H}_2$ ) is the ideal matrix for high-resolution ESR spectroscopy [15–24] for two reasons, as follows: first,  $p\text{-H}_2$  molecules in solid  $p\text{-H}_2$  have large zero-point vibrational motion due to their light mass and small intermolecular interactions, which repairs cracks, distortions, and imperfections, which thus keep the

solid highly homogeneous without annealing [6,7,15–17]. Second, since  $p\text{-H}_2$  has no nuclear spin moment, line broadening due to superhyperfine interaction can be avoided using purified  $p\text{-H}_2$  matrix [16–18]. We have reported highly resolved ESR lines of H [16],  $\text{CH}_3$  [18],  $\text{C}_2\text{H}_5$  [17],  $e^-$  [19,20], and  $\text{H}_6^+$  [20–23] in solid  $p\text{-H}_2$ .

$\text{H}_6^+$  is the radical ion, whose spectroscopic data were first reported by our group using the technique of high-resolution ESR spectroscopy with  $p\text{-H}_2$  matrices [20–23]. We have recently carried out isotopic substitution experiments and then confirmed the assignment [23]. Fig. 1(a) shows geometry of  $\text{H}_6^+$  calculated by Kurosaki and Takayanagi [25,26]. The  $\text{H}_6^+$  ion has  $\text{H}_2^+$ -core on the main axis sandwiched between chemically bound two side-on  $\text{H}_2$  groups. Isotropic hyperfine-coupling constants (HFCCs)  $A^{\text{iso}}$  experimentally determined show excellent agreement with those calculated, indicating that the calculation properly optimizes the geometry of  $\text{H}_6^+$  (see Table 1).

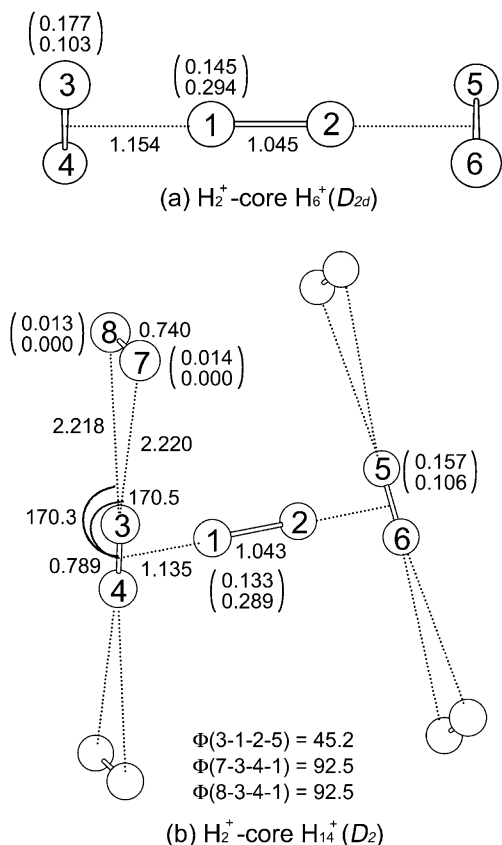
Anisotropic HFCCs,  $A^{\text{ani}}$ , however, differ greatly from the theoretical ones. Recently, we carried out ESR measurements on  $\text{H}_6^+$  and  $\text{H}_4\text{D}_2^+$ , both at 4.2 and 1.7 K, to conclude that the difference should be due to large precessional motion. In this paper, we present the ESR results and discuss possible precessional modes in solid  $p\text{-H}_2$ .

## 2. Experiment

$p\text{-H}_2$  (>99.5 mol %) was obtained by immersing iron hydroxide  $\text{FeO}(\text{OH})$  into liquid normal  $\text{H}_2$  (>99.99999%; Taiyo Nippon Sanso

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**Fig. 1.** Optimized geometries of  $H_6^+$  and  $H_{14}^+$  at the MP2/cc-pVTZ level reported by Kurosaki and Takayanagi [26]. Bond lengths in Å and angles in degrees. In parentheses are shown atomic net charge and spin density in the upper and lower lines, respectively.

**Table 1**

$A^{\text{iso}}$  and  $A^{\text{ani}}$  in mT of  $H_6^+$  and  $H_4D_2^+$  in solid p- $H_2$  at 4.2 K experimentally determined, and of  $H_6^+$  calculated

Level of calculation	$A^{\text{iso}}$		$A^{\text{ani}}$
	$H_2^+$ -core	Side-on $H_2$ ( $D_2$ )	
Experiment, $H_6^+$ at 4.2 K [23]	20.42	<sup>b</sup>	−0.06
Experiment, $H_4D_2^+$ at 4.2 K [23]	21.83, 19.43	(9.38) <sup>a, b</sup>	−0.12
MP2/cc-pVTZ [26]	19.690	8.745	
B3LYP/6-311++G(3df,3pd) [21]	20.079	10.263	1.17
MP2/cc-pVQZ [23]	20.231	9.007	1.25

<sup>a</sup> Multiplied by magnetomechanical ratio of proton to deuteron  $\gamma_p/\gamma_d = 6.514$ .

<sup>b</sup> Values for side-on  $H_2$  in  $H_6^+$  and  $H_4D_2^+$  cannot be observed due to free rotation [23].

Co.) for 10 h at 14 K. Ortho- $D_2$  (o- $D_2$ ) is purified from normal  $D_2$  (99.95%; Isotec Inc.) in the same manner at 18 K. The p- $H_2$  gas and p- $H_2$  containing o- $D_2$  at 1 mol % were sealed in a quartz ESR sample cell together with He (99.9999%; Taiyo Nippon Sanso Co.) at 0.1 mol %, introduced into a quartz ESR Dewar filled with liquid helium to produce solid p- $H_2$  at the bottom tip, and then irradiated with  $\gamma$ -rays for  $\sim 1$  h to a total dose of 2.88 kGy at the  $^{60}\text{Co}$   $\gamma$ -ray irradiation facility at Nagoya University. The irradiated p- $H_2$  sample with the Dewar was used with a commercial X-band ESR spectrometer (JEOL JES-RE1X). Temperatures were regulated by pumping liquid helium in the quartz Dewar as measured by a Au-Fe/Chromel thermo couple (The Nilaco Co.). Microwave frequency and magnetic field were monitored by the microwave frequency counter (Hewlett-Packard, 53150A) and NMR field meter (Echo Electronics Co. Ltd., EFM-2000AX), respectively.

### 3. Result

Fig. 2(a) shows the quartet ESR lines (B1–B4) of  $H_6^+$  ions in irradiated solid p- $H_2$ . The splitting of  $H_6^+$  lines is due to hyperfine interaction with the  $H_2^+$ -core nuclei [21–23]. The stick diagram shows resonance magnetic fields obtained by substituting the  $g$ -value  $g = 2.002$ , the isotropic HFCC for  $H_2^+$ -core  $A^{\text{iso}} = 20.44$  mT, and a nuclear spin moment of  $H_2^+$ -core and its  $z$ -component  $\{I_{1z}, I_{12z}\} = \{0, 0\}, \{1, -1\}, \{1, 0\}$  and  $\{1, 1\}$  in

$$\frac{h\nu}{g\mu_B} = H_0 + A^{\text{iso}}I_{12z} + \frac{A^{\text{iso}^2} \{I_{12}(I_{12} + 1) - I_{12z}^2\}}{2H_0}, \quad (1)$$

where suffixes of 1 and 2 express the positions of atoms in  $H_6^+$  in Fig. 1(a).

The equation with these parameters completely reproduces the line positions. On the other hand, hyperfine splitting due to side-on  $H_2$  groups was not observed, because the side-on  $H_2$  groups near temperature 4 K are in the ground rotational state  $J_{34} = J_{56} = 0$  around main axis of  $H_6^+$ , which is coupled to the  $I_{34} = I_{56} = 0$  nuclear spin states.

Fig. 3 shows ESR lines of  $H_6^+$  at  $I_{12z} = \pm 1$  named B3 and B4, respectively. The asymmetric lineshape in B3 and B4 is a typical powder-pattern shape with a uniaxial asymmetric hyperfine interaction. HFCC  $A$  is composed of an isotropic Fermi contact term  $A^{\text{iso}}$  and anisotropic dipolar–dipolar interaction one  $A^{\text{ani}}$  [11,12],

$$A = A^{\text{iso}} + (3 \cos^2 \theta - 1)A^{\text{ani}}, \quad (2)$$

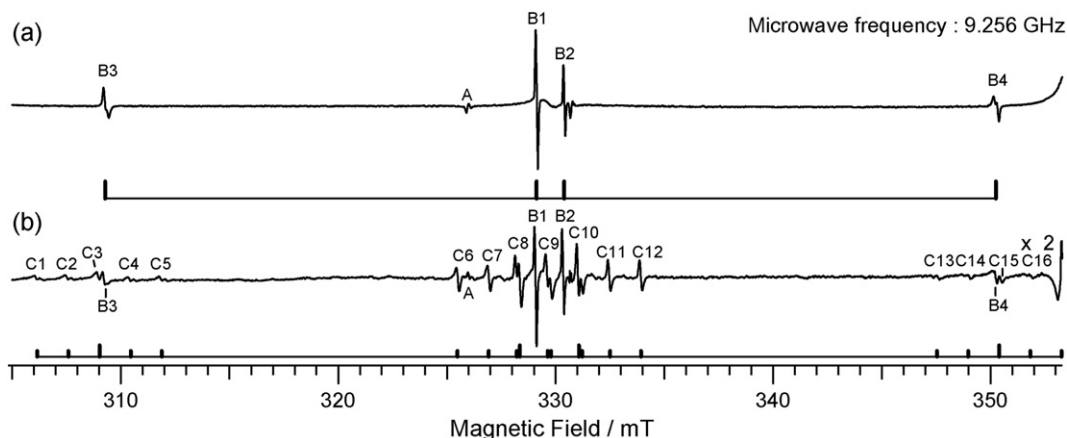
for radicals having uniaxial asymmetry, where  $\theta$  is the angle with respect to magnetic field  $H_0/z$ .  $A^{\text{iso}}$  determines line positions, and  $A^{\text{ani}}$  gives lineshape. The dotted lines in Fig. 3 show the simulated powder-pattern spectrum of  $H_6^+$  with  $A^{\text{ani}} = -0.06$  mT. The B3 and B4 lines measured both at 4.2 and 1.7 K are completely reproduced. The larger peaks in B3 and B4 are of  $H_6^+$  for  $\theta = 90^\circ$ , and smaller ones are for  $0^\circ$ . However, as shown in Table 1, theory has predicted  $A^{\text{ani}} = 1.17$ – $1.25$  mT, positive and much larger than that experimentally determined by a factor of  $-20$ .

Fig. 2(b) shows ESR spectra of  $H_2^+$ -core  $H_4D_2^+$  (C1–C16 (see Fig. 4)) produced in irradiated solid p- $H_2$  containing ortho- $D_2$  (o- $D_2$ ) at 1 mol %. Each of B1–B4 lines of  $H_6^+$  is split into quintets in the  $H_4D_2^+$  spectra due to hyperfine interaction with side-on  $D_2$ , which has  $I_{56} = 0$  and 2 nuclear spin quantum numbers at  $J_{56} = 0$  rotational state [23]. The stick diagram in Fig. 2(b) shows resonance fields of  $H_4D_2^+$  obtained by substituting  $g = 2.002$ ,  $A_{12}^{\text{iso}} = (A_1^{\text{iso}} + A_2^{\text{iso}})/2 = 20.63$  mT,  $\Delta A_{12}^{\text{iso}} = (A_1^{\text{iso}} - A_2^{\text{iso}})/2 = 1.2$  mT, isotropic HFCC of side-on  $D_2$ ,  $A_D^{\text{iso}} = 1.44$  mT, and  $z$ -component of nuclear spin quantum numbers of nuclei 1 and 2 in  $H_2^+$ -core, and side-on  $D_2$ ,  $I_{1z} = \pm 1/2$ ,  $I_{2z} = \pm 1/2$ ,  $I_{56z} = \pm 2, \pm 1, 0$  in

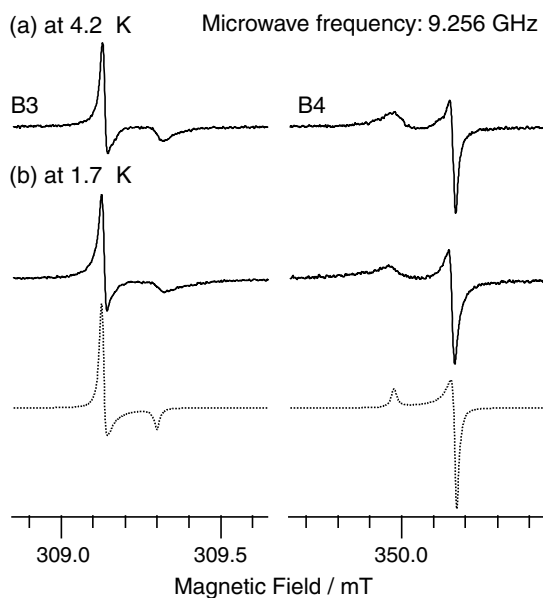
$$\frac{h\nu}{g\mu_B} = H_0 + A_{12}^{\text{iso}}(I_{1z} + I_{2z}) + \frac{A_{12}^{\text{iso}^2}}{2H_0}(I_{1z} - I_{2z}) \sqrt{\Delta A_{12}^{\text{iso}^2} + \left(\frac{A_{12}^{\text{iso}^2}}{2H_0}\right)^2} + A_D^{\text{iso}}I_{56z}. \quad (3)$$

The line positions are completely reproduced [23].  $\Delta A_{12}^{\text{iso}}A$  is due to small difference in amplitude of zero-point motion between side-on  $H_2$  and  $D_2$  in  $H_4D_2^+$  [28,29].

Fig. 4 shows C1–C5 and C13–C16 lines of  $H_4D_2^+$  for  $I_{12z} = I_{1z} + I_{2z} = \pm 1$ . The C1–C5 and C13–C16 lines of  $H_4D_2^+$  also look broadened by  $A^{\text{ani}}$ . The  $H_4D_2^+$  lines at 4.2 K are reproduced by the simulated spectrum with  $A^{\text{ani}} = -0.12$  mT, which is twice that for  $H_6^+$ , but much less than the theoretical result by a factor of  $-10$ . Unlike  $H_6^+$ ,  $H_4D_2^+$  was remarkably changed both in line positions and shapes by the decrease in temperature from 4.2 to 1.7 K. The C1–C5 (C13–C16) lines were shifted to upper (lower) fields by 1.2 mT. In addition, although upper (lower) peaks were more



**Fig. 2.** ESR spectra of  $H_6^+$  (B1–B4) and  $H_4D_2^+$  (C1–C16) in  $\gamma$ -ray irradiated solid (a) p- $H_2$  and (b) p- $H_2$  containing o- $D_2$  at 1 mol % at 4.2 K with field-modulation frequency of 50 kHz, its amplitude of 0.1 mT, and microwave power of 1 mW reported by Kumagai et al. [23]. B1–B4 lines are of  $H_6^+$ , and C1–C16 ones are of  $H_2^+$ -core  $H_4D_2^+$  [23]. The broad line at 330 mT is from irradiated quartz sample cell and Dewar. The line at 332 mT named A is forbidden transition of H atoms. The signals below 305 mT and above 353 mT could not be measured due to very intense H-atom lines. Note that the B1–B4 lines in (a) and (b) are saturated in intensity due to overpower and broadened due to overmodulation. The B1–B4 lines in solid p- $H_2$  measured with optimized microwave power and field-modulation amplitude are shown in Refs. [21,24]. Stick diagrams show resonance magnetic fields for  $H_6^+$  in (a) and  $H_4D_2^+$  in (b), respectively.



**Fig. 3.** ESR lines of  $H_6^+$  at  $I_{2z} = \pm 1$  (B3 and B4) in  $\gamma$ -ray irradiated solid p- $H_2$  measured with field-modulation frequency of 50 kHz, its amplitude of 0.01 mT, and microwave power of 1 mW for (a) and 0.4 mT for (b). The dashed line is a simulated spectrum of  $H_6^+$  with  $A_0^{\text{ani}} = -0.06$  mT.

intense than the lower (upper) in the C1–C5 (C13–C17) lines at 4.2 K; the lower (upper) ones became more intense at 1.7 K.

The change in lineshape of C1–C5 and C13–C17 can be explained by the change in  $A^{\text{ani}}$ . The spectrum is reproduced by the simulated one in Fig. 4(b) with  $A^{\text{ani}} = 1.17$  mT, which is positive and very close to the theoretical values. The smaller peaks of C1–C5 and C13–C17 lines of  $H_4D_2^+$  for  $\theta = 0^\circ$  disappeared at 1.7 K probably due to poor signal-to-noise ratio.

Note that we have not observed any feature due to anisotropic hyperfine interaction with side-on  $D_2$  nuclei in  $H_4D_2^+$ , which causes difference in lineshape and width among C1–C5 and C13–C17. Theory also predicted that the anisotropic HFCC of side-on  $D_2$  should be much less than that of  $H_2^+$ -core by a factor of  $\sim 10$  [23]. Therefore, we ignored it in the analysis of  $H_4D_2^+$  lines.

#### 4. Discussion

We propose that the discrepancy in  $A^{\text{ani}}$  between experiment and theory should be due to the local motion of  $H_6^+$  and  $H_4D_2^+$  in each cage of solid p- $H_2$ . Although theory calculates the anisotropic HFCC  $A_0^{\text{ani}}$  against the molecular axes, ESR measures projection of  $A_0^{\text{ani}}$  on crystalline axes. Theoretical values can be compared with experimental ones only when radicals are fixed in the crystalline axes. The  $A^{\text{ani}}$  values should decrease with the increase in amplitude of precession or libration due to the motional narrowing effect.

Suppose that a radical has a precessional motion around a crystalline axis in the  $y$ - $z$  plane with the precessional angle  $\theta$ , where the unit vector  $r$  of the main axis of radical is given by

$$r(\theta, \varphi, \Theta) = \begin{pmatrix} r_x \\ r_y \\ r_z \end{pmatrix} = \begin{pmatrix} 1 & 0 & 0 \\ 0 & \cos \Theta & -\sin \Theta \\ 0 & \sin \Theta & \cos \Theta \end{pmatrix} \begin{pmatrix} \cos \varphi \sin \theta \\ \sin \varphi \sin \theta \\ \cos \theta \end{pmatrix} \quad (4)$$

$$= \begin{pmatrix} \cos \varphi \sin \theta \\ \cos \Theta \sin \varphi \sin \theta - \sin \Theta \cos \theta \\ \sin \Theta \sin \varphi \sin \theta + \cos \Theta \cos \theta \end{pmatrix},$$

with the phase of precession  $\varphi$ .  $A^{\text{ani}}(\theta, \varphi, \Theta)$ , anisotropic HFCC at  $\theta$ ,  $\theta$ , and phase  $\varphi$ , are related by

$$A^{\text{ani}}(\theta, \varphi, \Theta) = (3r_z^2 - 1)A_0^{\text{ani}}. \quad (5)$$

The expected value for  $A^{\text{ani}}(\theta, \varphi, \Theta)$  in the precessional motion, is given by averaging  $A^{\text{ani}}(\theta, \varphi, \Theta)$  around  $\varphi$ ,

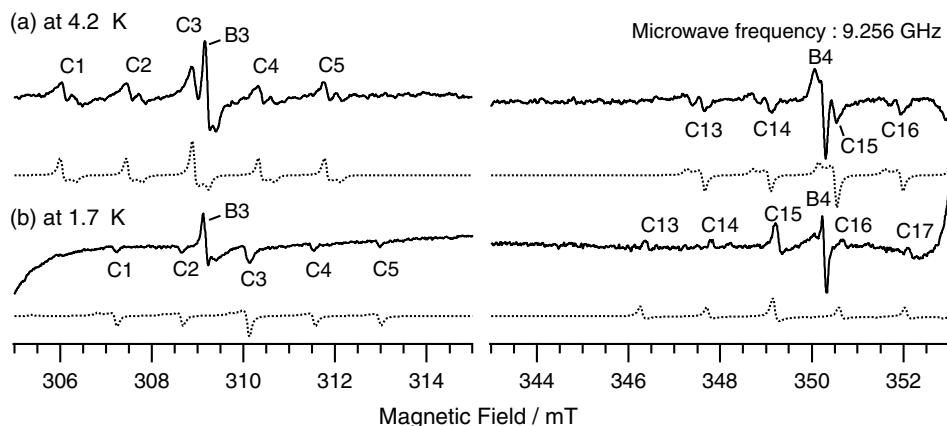
$$A_{\text{pre}}^{\text{ani}}(\theta, \Theta) = \frac{\int_0^{2\pi} (3r_z^2 - 1)A_0^{\text{ani}} d\varphi}{\int_0^{2\pi} d\varphi} \quad (6)$$

$$= \frac{3 \cos^2 \theta - 1}{2} (3 \cos^2 \theta - 1)A_0^{\text{ani}}$$

$$\equiv (3 \cos^2 \theta - 1)A_{\text{pre}}^{\text{ani}}(\theta).$$

$\theta = 0^\circ$  corresponds to radicals completely fixed relative to crystalline axes, and  $\theta = 90^\circ$  means that each radical rotates in a plane. The anisotropy measured by ESR is  $A_0^{\text{ani}}(\theta)$  related to  $A_0^{\text{ani}}$  by

$$A_{\text{pre}}^{\text{ani}}(\theta) = \frac{3 \cos^2 \theta - 1}{2} A_0^{\text{ani}} \quad (6')$$



**Fig. 4.** ESR lines of  $\text{H}_4\text{D}_2^+$  at  $I_{12z} = \pm 1$  (C1–C5 and C13–C17) in  $\gamma$ -ray irradiated solid p- $\text{H}_2$  containing o- $\text{D}_2$  at 1 mol % with field-modulation frequency of 50 kHz, its amplitude of 0.1 mT, and microwave power of 1 mW for (a) and 0.4 mT for (b). The dashed lines are simulated spectra of  $\text{H}_4\text{D}_2^+$  with  $A^{\text{ani}} = -0.12$  mT for (a) and 1.17 mT for (b).

is deduced.  $A_{\text{pre}}^{\text{ani}}(\theta)$ , which is equal to  $A_0^{\text{ani}}$  at  $\theta = 0^\circ$ , decreases with increasing  $\theta$  to be  $-A_0^{\text{ani}}/2$  at  $90^\circ$ , and crosses 0 at the magic angle of  $54.74^\circ$ .

On the other hand, when the radical is in librational motion with the maximum librational angle  $\theta$ , the expected value,  $A_{\text{lib}}^{\text{ani}}(\theta, \Theta)$ , is given by,

$$\begin{aligned} A_{\text{lib}}^{\text{ani}}(\theta, \Theta) &= \frac{\int_0^\theta \int_0^{2\pi} (3r_z^2 - 1) A_0^{\text{ani}} d\varphi \sin\theta d(\theta)}{\int_0^\theta \int_0^{2\pi} d\varphi \sin\theta d\theta} \\ &= A_0^{\text{ani}} \frac{\cos\theta(1 + \cos\theta)}{2} (3\cos^2\theta - 1) \\ &\equiv A_{\text{lib}}^{\text{ani}}(\theta) (3\cos^2\theta - 1). \end{aligned} \quad (7)$$

$A_{\text{lib}}^{\text{ani}}(\theta)$ , corresponding to  $A_0^{\text{ani}}$  at  $\theta = 0^\circ$ , decreases with an increase in  $\theta$  to be 0 at  $90^\circ$ , which corresponds to free rotational state. Unlike  $A_{\text{pre}}^{\text{ani}}(\theta)$ , the sign of  $A_{\text{lib}}^{\text{ani}}(\theta)$  cannot be negative for  $0^\circ \leq \theta \leq 90^\circ$  and  $A_0^{\text{ani}} > 0$ . Therefore, a negative value of  $A^{\text{ani}}$  in  $\text{H}_6^+$  at 4.2 and 1.7 K, and  $\text{H}_4\text{D}_2^+$  at 4.2 K should be due to a large precessional motion with  $\theta > 54.74^\circ$ , but not due to libration!

We determined  $\theta$  in Table 2 by substituting the experimental value of  $A^{\text{ani}}$  to  $A_{\text{pre}}^{\text{ani}}(\theta)$ , and the theoretical one to  $A_0^{\text{ani}}$  in Eq. (6), respectively.  $\theta = 57^\circ$  is obtained for  $\text{H}_6^+$  at 4.2 and 1.7 K, and  $59^\circ$  for  $\text{H}_4\text{D}_2^+$  at 4.2 K, but only  $12^\circ$  for  $\text{H}_4\text{D}_2^+$  at 1.7 K.

Let us consider possible precessional mode of  $\text{H}_6^+$  and  $\text{H}_4\text{D}_2^+$  in solid p- $\text{H}_2$ . Fig. 1(b) shows the optimized geometry of  $\text{H}_{14}^+$  [26]. Since  $\text{H}_{14}^+$  is composed of  $\text{H}_6^+$  and physically bound outer four  $\text{H}_2$ s we can use the outer  $\text{H}_2$ s to resemble  $\text{H}_2$  molecules around  $\text{H}_6^+$  in solid p- $\text{H}_2$ . The equilibrium  $\text{H}_6^+ - \text{H}_2$  distance is 3.2 Å, which is close to the intermolecular distance of solid p- $\text{H}_2$  (3.793 Å [27]). Therefore,  $\text{H}_6^+$  should be trapped in a single substitutional cage of solid p- $\text{H}_2$ .

Fig. 5 shows a model of  $\text{H}_6^+$  trapped in a single substitutional hcp cage of solid p- $\text{H}_2$ . The cage has 8 triangular and 6 square planes.

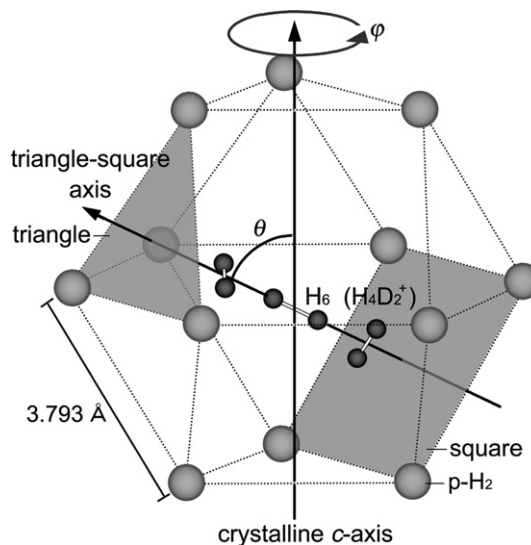
**Table 2**

$A^{\text{ani}}$  and  $\theta$  of  $\text{H}_6^+$  and  $\text{H}_4\text{D}_2^+$  in solid p- $\text{H}_2$

	Temperature/K	$A^{\text{ani}}/\text{mT}$	$\theta^{\text{b}}/\text{degree}$
$\text{H}_6^+$	4.2	-0.06	57
	1.7	-0.06	57
$\text{H}_4\text{D}_2^+$	4.2	-0.12	59
	1.7	1.17	12
Theory <sup>a</sup>		1.25	

<sup>a</sup> Theoretical value is obtained at the MP2/cc-pVQZ level of calculation.

<sup>b</sup> Precession angle  $\theta$  obtained by substituting experimental value in  $A_{\text{pre}}^{\text{ani}}$  and theoretical one in  $A_0^{\text{ani}}$  of Eq. (6) (see text).



**Fig. 5.** Schematic representation of  $\text{H}_6^+$  trapped in a single substitutional hcp cage of solid p- $\text{H}_2$ .

All triangular planes at the side diagonally face to the square ones, but the triangular plane at the top faces to the triangular one at the bottom. We propose that the main axis of  $\text{H}_6^+$  should be along the axis passing through centers of a pair of diagonally faced square and triangle planes (triangle-square axis) in order to avoid overlap of electronic orbital between  $\text{H}_6^+$  and p- $\text{H}_2$ s. When  $\text{H}_6^+$  in the axis is off-centered from the center of cages to the square by 0.3 Å, the distances between side-on  $\text{H}_2$  of  $\text{H}_6^+$  to each p- $\text{H}_2$  molecule at the apexes of triangle and square are calculated to be 2.8 Å. This value is very close to the distance between a side-on  $\text{H}_2$  of  $\text{H}_6^+$  and an outer  $\text{H}_2$  in Fig. 1(b) of 2.6 Å. Eventually, these values should be larger than 2.6 Å when the effect of nuclear quantum fluctuation is taken into account on the calculation [28,29]. This result indicates that  $\text{H}_6^+$  should be trapped along the triangle-square axis with little distortion of the hcp cage of solid p- $\text{H}_2$ .

On the other hand, when  $\text{H}_6^+$  is aligned along the c-axis of solid p- $\text{H}_2$ , the distance between side-on  $\text{H}_2$  and p- $\text{H}_2$  molecules at the apexes of upper and lower triangles is 2.6 Å, being a little shorter than the equilibrium distance expected when taking into account the nuclear quantum fluctuation. Therefore,  $\text{H}_6^+$  should prefer the triangle-square axes rather than c-axis.

We suggest that the  $\text{H}_6^+$  ions are in precessional motion along c-axis by jumping among the six equivalent triangle-square axes



in solid p-H<sub>2</sub>. When the cage is not distorted, the angle between *c*-axis and triangle-square axis in the hcp cage is calculated to be  $\theta_{\min} = 63.2^\circ$ , which is very close to the precessional angle of H<sub>6</sub><sup>+</sup> at 4.2 and 1.7 K (57°), and H<sub>4</sub>D<sub>2</sub><sup>+</sup> at 4.2 K (59°) determined experimentally.

The similar values of  $A^{\text{ani}}$  between experiment and theory in H<sub>4</sub>D<sub>2</sub><sup>+</sup> at 1.7 K indicate that the precessional motion is stopped. Why is the precessional motion stopped in H<sub>4</sub>D<sub>2</sub><sup>+</sup> but not in H<sub>6</sub><sup>+</sup>? We propose two possible reasons as follows: first, the moment of inertia for H<sub>4</sub>D<sub>2</sub><sup>+</sup> is larger than that for H<sub>6</sub><sup>+</sup>. H<sub>4</sub>D<sub>2</sub><sup>+</sup> is heavier than H<sub>6</sub><sup>+</sup>, and, unlike H<sub>6</sub><sup>+</sup>, the center of mass does not coincide with the center of geometry in H<sub>4</sub>D<sub>2</sub><sup>+</sup>. Second, not only the nuclear configuration but also the electronic wave function of H<sub>4</sub>D<sub>2</sub><sup>+</sup> no longer has *D*<sub>2d</sub> symmetry but has *C*<sub>2v</sub> [23]. This means that the energy  $E(\theta_{\min}, \varphi)$  of H<sub>4</sub>D<sub>2</sub><sup>+</sup> in the hcp cage of solid p-H<sub>2</sub> does not have 6-fold but has 3-fold symmetry around  $\varphi$ . H<sub>4</sub>D<sub>2</sub><sup>+</sup> should be localized in one of three deeper potential wells at 1.7 K.

We have no idea whether the precession of H<sub>6</sub><sup>+</sup> is due to quantum mechanical tunneling or classical thermal hopping. Small mass and matching in energy levels between neighboring wells are essential for quantum tunneling. Because of the small moment of inertia and high symmetry, H<sub>6</sub><sup>+</sup> may keep the precession via the tunneling down to 0 K. On the other hand, the rate for the tunneling precession should be much less in H<sub>4</sub>D<sub>2</sub><sup>+</sup>, because of larger moment of inertia and lower symmetry in potential for precession.

In conclusion, we have compared anisotropic HFCC of H<sub>6</sub><sup>+</sup> and H<sub>4</sub>D<sub>2</sub><sup>+</sup> in solid p-H<sub>2</sub> determined by the analysis of ESR lines with theoretical calculation to find the results as follows: H<sub>6</sub><sup>+</sup> is in precessional motion at precessional angle of 57° along the *c*-axis of substitutional hcp cage in solid p-H<sub>2</sub> both at 4.2 and 1.7 K. Although H<sub>4</sub>D<sub>2</sub><sup>+</sup> is also in the precessional motion at 4.2 K, the precession is stopped at 1.7 K. The difference should be due to larger moment of inertia and lower molecular symmetry in H<sub>4</sub>D<sub>2</sub><sup>+</sup>.

Local environment of cages around guest molecules and their local motions should be determined in order to study solid-phase chemical reaction between guest and host molecules. Recently, we have observed the reactions related to H<sub>6</sub><sup>+</sup> such as H<sub>6</sub><sup>+</sup> + H<sub>2</sub> → H<sub>2</sub> + H<sub>6</sub><sup>+</sup> and H<sub>6</sub><sup>+</sup> + e<sup>-</sup> → 3H<sub>2</sub> in solid p-H<sub>2</sub>. We hope that the mechanism of solid-phase reactions related to H<sub>6</sub><sup>+</sup> can be clarified through this study.

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